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Doping-dependent optical properties of Bi2201

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Abstract. An experimental study of the in-plane optical conductivity of $(Pb_x, Bi_{2-x})(La_ySr_{2-y})CuO_{6+\delta}$ (Bi2201) is presented for a broad doping and temperature range. The in-plane conductivity is analyzed within a strong coupling formalism. We address the interrelationship between the optical conductivity ($\sigma(\omega)$), the single particle self-energy and the electron-boson spectral function. We find that the frequency and temperature dependence can be well described within this formalism. We present a universal description of optical, angle resolved photoemission spectroscopy (ARPES) and tunneling spectra. The full frequency and temperature dependence of the optical spectra and single particle self-energy is shown to result from an electron-boson spectral function, which shows a strong doping dependence and weak temperature dependence.

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1. Introduction

Many properties distinguish high-temperature superconductors from conventional superconductors; the most distinguishing property is of course the critical temperature. It is therefore not surprising that experimental and theoretical efforts are aimed at finding alternatives for the conventional electron-phonon coupling-driven pairing mechanism. The field is currently divided into two schools. The first school explains the peculiarities of these materials by strong correlation effects [1]–[5], while the second seeks the origin in the coupling of electrons to a spectrum of bosons [6]–[10]. The first school typically approaches the problem starting from doping the Mott-insulating state of the parent compounds. The resulting state of matter is not adiabatically connected with another well-known state of matter, the Fermi liquid; hence its properties are fundamentally different. The important interactions are then the on-site Coulomb repulsion U and the anti-ferromagnetic exchange coupling J, neither of which qualifies as a retarded interaction as in the standard Eliashberg framework [11]. The second school starts by assuming that the underlying state of matter is a Fermi liquid but that the peculiar properties arise due to a strong coupling of electrons to bosons different from phonons in ordinary metals, for example spin fluctuations.

A problem in the study of the electron–boson coupling in cuprates is the high critical temperature of these materials: since spectroscopic signatures of the interaction are smeared out by thermal broadening, they are more easily determined at low temperatures. However, a careful description of the superconducting (d-wave) state complicates the analysis tremendously. Nevertheless, some attempts have been made to extract the bosonic spectral function in the superconducting state [12]. The study of cuprates with a low critical temperature can therefore be of interest, because the analysis can be performed at low temperatures without the intervention of the superconducting state.

In a recent study, we reported on an analysis of the optical properties of several cuprates [13]. We found evidence for a broad, structured bosonic spectrum extending up to energies of 300–400 meV. The spectra consist of two features: (i) a robust peak in the range of 50–60 meV and (ii) a doping-dependent continuum extending to 300–400 meV for the samples with the highest T_c . Interestingly, the doping dependence of these spectra correlates with that of the critical temperature. In this paper, we report on the optical spectra of (Pb_x, Bi_{2-x})(La_ySr_{2-y})CuO_{6+ δ} (Bi2201) used in that study and discuss the analysis of [13] in more detail.

The structure of the paper is as follows. In section 2, we discuss the experimental techniques and optical conductivity. In section 3, the strong coupling formalism is introduced and we present the analysis of optical spectra within this formalism. In section 4, we make a comparison with angle-resolved photoemission spectroscopy (ARPES) and tunneling experiments within the context of a model unifying the results from both experimental techniques.

2. Experiments

The optical properties of four samples of Pb- and La-substituted Bi2201 are studied: underdoped Bi₂Sr_{1.25}La_{0.75}CuO_{6+ δ} (UD0, $T_c = 0$ K) and Pb_{0.5}Bi_{1.55}Sr_{1.2}La_{0.8}CuO_{6+ δ} (UD10, $T_c = 10$ K), optimally doped Pb_{0.55}Bi_{1.5}Sr_{1.6}La_{0.4}CuO_{6+ δ} (OpD35, $T_c = 35$ K) and overdoped Pb_{0.38}Bi_{1.74}Sr_{1.88}CuO_{6+ δ} (OD0, $T_c = 0$ K). Temperature-dependent experiments are performed in cryostats that have been specially adapted to keep the sample position fixed during thermal cycling. Far-infrared reflectivity experiments are carried out at pressures of about $p \approx 10^{-6}$ mbar, while the mid-infrared reflectivity and near infrared (IR)/ultraviolet ellipsometry experiments are carried out under ultra high vacuum conditions with $p \approx 10^{-9}$ mbar. Samples are freshly cleaved just before being inserted into the cryostat. For each sample, spectra were taken between 10 and 300 K with a temperature interval of 2 K. We use a Fourier-transform IR spectrometer for reflection experiments in the range 5–750 meV. The reference for the reflection measurements is taken on a gold film deposited *in situ* on the sample. Ellipsometric measurements are performed in the energy range 0.75–6 eV.

2.1. Normal incidence reflectivity

Reflectivity spectra are shown in figure 1 for all four samples at three temperatures: 10, 100 and 290 K. The reflectivity data are characteristic of a bad metal and show a strong doping dependence. With increasing doping the metallicity increases and the reflectivity increases accordingly. As a result the sharp phonon structures, which can be clearly seen in the UD0 sample (top right panel), become progressively more screened and are hardly visible in the OD0 spectra. The metallicity manifests itself in a dependence on frequency that follows the Hagen–Rubens trend $R(\omega) = 1 - \sqrt{2\rho_{dc}\omega/\pi}$ for frequencies below 25 meV (200 cm⁻¹). We made fits to the low-frequency reflectivity using the Hagen–Rubens expression to estimate the dc resistivity. The values obtained in this way are in agreement with those reported in the literature for similar doping values [14, 15] and the fits extrapolate to $R(\omega \rightarrow 0) = 1$ within our experimental uncertainty (±0.5%). The exception is the UD0 sample. On a qualitative level, the reflectivity looks similar to that of a disordered metal (for an example see [16]). The temperature

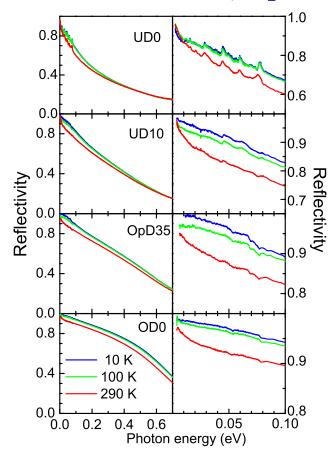


Figure 1. Reflectivity for four different dopings of Bi2201 at T = 10, 100 and 290 K. From top to bottom: UD0, UD10, OpD35 and OD0 samples. The left-hand panels show the reflectivity on a large scale, while the right-hand panels show the low-energy reflectivity highlighting the phonon range.

dependence is also somewhat different from the other samples: the reflectivity increases with decreasing temperature but below 10 meV the reflectivity first shows a small increase and then starts to decrease for temperatures below about 100 K.

2.2. Ellipsometry

Ellipsometric measurements give direct access to the complex pseudo-dielectric function, $\hat{\varepsilon}_{pseudo}(\omega)$, which corresponds closely to $\hat{\varepsilon}_{ab}(\omega)$ with a weak admixture of the *c*-axis component. Correspondingly, the transformation from $\hat{\varepsilon}_{pseudo}(\omega)$ to $\hat{\varepsilon}_{ab}(\omega)$ using the Fresnel equations gives rise to a small correction for the *c*-axis admixture in this frequency range. This has been verified for several high- T_c cuprates with roughly the same optical constants [17, 18]. The *c*-axis dielectric constant is almost independent of energy between 1.25 and 3 eV and is roughly equal to 4.1 for Bi2223 and 4.0 for Hg-1201. We use a frequency-independent *c*-axis dielectric constant for Bi2201, $\hat{\varepsilon}_c \approx 4.3$, to correct $\hat{\varepsilon}_{pseudo}(\omega)$. A systematic error for this procedure was determined by varying the value of $\hat{\varepsilon}_c$ between 4 and 4.5 and is indicated as the error bar in figure 2.

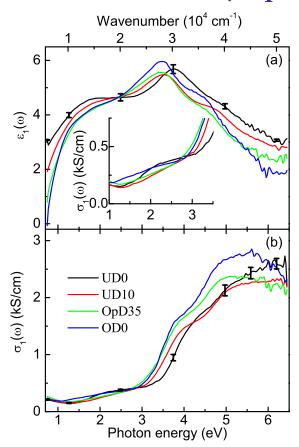


Figure 2. (a) Real part of the dielectric function, $\varepsilon_1(\omega)$. (b) Real part of the optical conductivity, $\sigma_1(\omega)$. We only display room temperature spectra, since the temperature dependence for these frequencies is almost indiscernible at this scale. The error bars shown for the UD sample are systematic error bars and are representative for all four samples.

The *c*-axis corrected functions obtained from the ellipsometric measurements, $\varepsilon_{1,ab}(\omega)$ and $\sigma_{1,ab}(\omega)$, are displayed in figure 2. We observe a series of interband transitions starting around 2 eV (see inset in figure 2(a)). At this energy there is a weak onset, which is most clearly pronounced for the UD0 sample, which has been associated with the onset of charge transfer excitations [19]. We observe three more transitions at higher energy that show a significant doping dependence.

2.3. In-plane conductivity

The combination of reflection experiments and ellipsometry makes the determination of the optical conductivity in the IR range more robust, as detailed in [20]. We display the optical conductivity, $\sigma_1(\omega)$, in figure 3 at several temperatures. As expected the low-frequency conductivity increases strongly with doping (note the factor of two difference in scale between the upper and lower panels). With the exception of the UD0 sample, the conductivities show a metallic Drude response. The UD0 sample shows a broad incoherent response with an interesting temperature dependence: with decreasing temperature an asymmetric peak develops with a maximum at 15–20 meV. A similar structure and temperature trend has also been

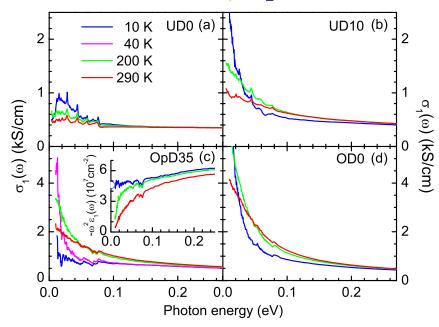


Figure 3. Optical conductivities for (a) UD0, (b) UD10, (c) OpD35 and (d) OD0 samples. Note the difference in scale between the upper and lower panels. For the OpD35 sample an extra curve is shown just above T_c . The inset in (c) shows an estimate of the superfluid density for the OpD35 sample. The open semi-circle corresponds to the estimate found from a Drude–Lorentz fit of the data.

observed for YBa₂Cu₃O_{6+ δ} (YBCO) [21], indicating that this is a generic feature of underdoped cuprates. The pronounced mid-infrared structure observed in [21] is less visible here. The optical conductivity of the OpD35 sample at T = 10 K does not show a clear signature of the superconducting gap, but the conductivity is strongly suppressed as compared to $\sigma_1(\omega)$ at T = 40 K. Another signature of superconductivity is the presence of a superfluid density, which appears as a $\delta(\omega)$ -function in $\sigma_1(\omega)$ with strength $\omega_{p,s}$. $\omega_{p,s}^2$ is directly proportional to the superfluid density and can be estimated from a Drude–Lorentz fit. We find $\omega_{p,s} \approx 0.84$ eV. As a double check we use the fact that, due to causality, the delta function in $\sigma_1(\omega)$ gives rise to a contribution to $\varepsilon_1(\omega) \approx -\omega_{p,s}^2/\omega^2$. The inset in figure 3(c) compares the superfluid density obtained by extrapolating $-\omega^2 \varepsilon_1(\omega)$ to zero frequency to the one obtained from the Drude–Lorentz fit, shown as a semi-circle. The two estimates are in good agreement. The superfluid density is substantially smaller than that of optimally doped Bi2212 [22] $(\omega_{p,s} \approx 1.18 \text{ eV})$ and Bi2223 [17] $(\omega_{p,s} \approx 1.28)$ but T_c is correspondingly lower. This correlation between T_c and the superfluid density has been observed by several authors [23, 24].

3. Analysis

3.1. The extended Drude model

The Drude model describes the optical conductivity of a gas of non-interacting electrons with a single, energy-independent channel of dissipation: $4\pi \hat{\sigma}(\omega) = \omega_p^2/(1 - i\omega\tau)$. This model is insufficient to describe the situation where the dissipation in the electron system arises from

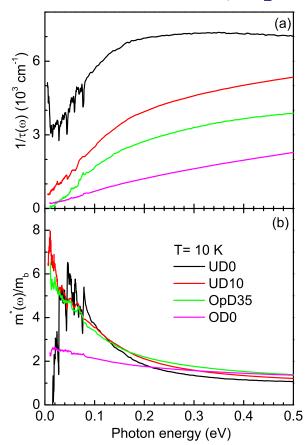


Figure 4. Scattering rate, $1/\tau(\omega)$, and effective mass, $m^*(\omega)/m_b$, at T = 10 K. Note the upturn in the UD0 scattering rate, which indicates that the data cannot be described within this formalism.

the electron-phonon or electron-electron interactions. To deal with these situations we can generalize the Drude model by introducing a memory function $\hat{M}(\omega)$ [25],

$$\hat{\sigma}(\omega) \equiv \frac{\omega_{\rm p}^2}{4\pi} \frac{\rm i}{(\omega + \hat{M}(\omega))},\tag{1}$$

or 'optical self-energy' $(2\hat{\Sigma}_{op}(\omega) = -\hat{M}(\omega))$ [9]. Two related quantities are the effective mass, $m^*(\omega)/m = M_1(\omega)/\omega + 1$, and scattering rate, $1/\tau(\omega) = M_2(\omega)$. These quantities are useful because they are more easily interpreted physically. Equation (1) is easily inverted to obtain the scattering rate $1/\tau(\omega)$ and effective mass $m^*(\omega)/m_b$ directly from the measured conductivity, provided one has an estimate of the plasma frequency, ω_p , and the contribution due to interband transitions ε_{∞} [18, 26]. $1/\tau(\omega)$ and $m^*(\omega)/m_b$ are shown in figure 4 at T = 10 K. The UDO sample has the highest scattering rate and strongest frequency dependence. However, $1/\tau(\omega)$ shows an upturn at low frequency and a corresponding negative effective mass in the same frequency range. The implication of this is that the low-temperature, low-frequency properties cannot be described in terms of an interacting gas of electrons and thus invalidates the extended Drude analysis for this compound. A similar observation was made in [21] for heavily

underdoped YBCO samples. However, the scattering rate reported there shows a peak structure around 150 meV, which is not found here.

The other three samples show monotonically increasing scattering rates, except in the vicinity of direct optical phonon absorptions. The overall scattering rate as well as the magnitude of the frequency dependence strongly decreases with increasing doping. This can be related to a decreasing coupling to low energy bosonic excitations. A measure of this coupling strength can be obtained from the relation $m^*/m_b(\omega \rightarrow 0) = \lambda + 1$. Therefore λ can be estimated directly from figure 4(b), showing that λ decreases from $\lambda \approx 6.5$ for UD10 to $\lambda \approx 1.5$ for the OD0 sample. The room temperature values for the three samples are $\lambda_{\text{UD10}} \approx 4.5$, $\lambda_{\text{OpD35}} \approx 3$ and $\lambda_{\text{OD0}} \approx 1.5$. The determination of these coupling strengths from experimental quantities will serve as an important consistency check in section 3.2.

3.2. Strong coupling formalism

In this section, we will focus on the memory function because of its relation to selfenergies above and below the Fermi energy and because structures arising from electron-boson interactions are more clearly visible in $M_1(\omega)$ than in $m^*(\omega)/m_b$ and $1/\tau(\omega)$ [9, 10]. Encoded in the memory function are the self-energy effects associated with the electron-electron and electron-phonon interaction. The relation between single particle self-energies and the memory function is given by [27]–[29]

$$\frac{\hat{M}(\omega,T)}{\omega} = \left[\int_{-\infty}^{+\infty} \frac{\left[f(\omega+\varepsilon,T) - f(\varepsilon,T) \right] d\varepsilon}{\omega - \Sigma(\varepsilon+\omega,T) + \Sigma^*(\varepsilon,T)} \right]^{-1} - 1,$$
(2)

where $f(\varepsilon, T)$ are Fermi factors and $\Sigma(\omega)$ and $\Sigma^*(\omega)$ are self-energies above and below the Fermi energy. To arrive at this result we have to make some assumptions. First, we neglect vertex corrections and the energy dependence of the density of states. Furthermore, the self-energies are assumed to be momentum-independent. We will return to this latter assumption in section 4. Under these circumstances we can express the single particle self-energy as

$$\Sigma(\omega, T) = \int d\varepsilon \int d\omega' \tilde{\Pi}(\omega') \left[\frac{n(\omega') + f(\varepsilon)}{\omega - \varepsilon + \omega' + i\delta} + \frac{n(\omega') + 1 - f(\varepsilon)}{\omega - \varepsilon - \omega' - i\delta} \right]$$
(3)

with Bose factors, $n(\varepsilon, T)$, and the 'glue function', $\Pi(\omega)$. The tilde on this quantity indicates that it is an effective spectral density that potentially contains features not arising from coupling to bosons, for example the opening of a pseudogap in the density of states. Several authors have discussed the applicability of this formalism and its underlying assumptions to the cuprate problem [11], [30]–[33]. We want to determine whether or not it can be consistently applied to the optical properties of cuprates and see the implications of the resulting glue-functions with regard to other experimental probes.

Several microscopic theories give predictions about the shape of $\Pi(\omega)$. We have tested these predictions, as well as 'model-independent' functions, for HgBa₂CuO_{4+ δ} as described in [34]. We use a histogram representation of $\Pi(\omega)$ using N blocks with adjustable positions and heights,

$$\Pi(\omega) = f_i, \quad \omega_{i-1} \leqslant \omega \leqslant \omega_i, \tag{4}$$

where *i* runs from 1 to *N*, $\omega_0 = 0$ and f_i is the height of the *i*th block. For $\omega_0 \le \omega \le \omega_1$ we use $\tilde{\Pi}(\omega) = f_1 \omega$ to circumvent the divergence of the integral in (3). The 2*N* parameters

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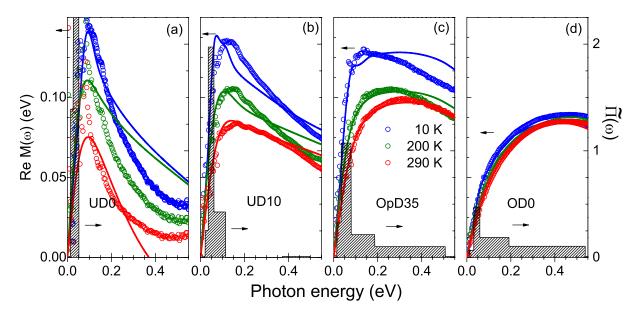


Figure 5. Memory function $\hat{M}(\omega)$ (symbols) together with calculated quantities (solid lines). The shaded area corresponds to the room temperature $\tilde{\Pi}(\omega)$ function used in the calculations.

of this model are optimized using a standard Levenberg–Marquardt least square routine. This routine optimizes the parameters of the histogram model to obtain the best fit to the experimental reflectivity and ellipsometry data. The resulting histogram gives an indication of the important features in the spectrum. We find that the detail of $\Pi(\omega)$ that can be extracted from the experimental data is best represented with N = 6 blocks. For cuprates the function $\Pi(\omega)$ consists of two main features: a peak with an energy in the range 50–60 meV and a broad spectrum extending up to 400 meV [13].

3.3. Temperature dependence of the self-energy/memory function

Equations (2) and (3) depend on temperature through the Bose and Fermi factors only. In the electron-phonon problem the temperature dependence of the phonon spectral density is very weak, and can be neglected. However, if the bosons that make up $\Pi(\omega)$ derive from electronic degrees of freedom $\Pi(\omega)$ can depend on temperature due to feedback effects [32]. In [13], we found that a fit of the experimental data at all temperatures required a temperature-dependent $\Pi(\omega)$, suggesting that it derives at least in part from electronic degrees of freedom. In figure 5, the room temperature $\Pi(\omega)$ spectra are reproduced together with experimental and calculated memory functions for the four samples. The experimental memory functions show a strong doping dependence from narrow and strongly peaked in the underdoped regime to broad with no clear maximum on the overdoped sample. The comparison with the $\Pi(\omega)$ function shows that the presence of this maximum correlates with the strength of the peak at 50–60 meV in the $\Pi(\omega)$ function. We use the $\Pi(\omega)$ spectrum that gives the best fit to the room temperature optical spectra to calculate the memory function at several temperatures. At room temperature the calculated $\hat{M}(\omega)$ is therefore the best fit to the experimental one based on (2) and (3).

The reason for choosing the room temperature $\Pi(\omega)$ is that at lower temperatures the spectra might contain features related to the pseudogap. The quality of the fit becomes progressively worse with decreasing doping. For the most underdoped sample, UD0, the room temperature data can no longer be described by this formalism. So we may conclude that (i) equations (2) and (3) describe well the state of affairs in optimally and overdoped superconductors and (ii) the equations fail miserably for the most underdoped sample. This could imply a doping-induced transition between two different states of matter, non-Fermi liquid on the underdoped side and Fermi liquid on the overdoped side. The exact doping value separating these two regimes is difficult to establish beyond any question with this method: the fits and temperature dependence may still be rather good if the system is only slightly away from the Fermi liquid regime.

3.4. Temperature dependence of $\tilde{\Pi}(\omega)$

 $\hat{M}(\omega)$ is calculated at 10 and 200 K by correspondingly changing temperature in (2) and (3) but using the same $\Pi(\omega)$ as for 290 K. It is clear from figure 5 that most of the temperature dependence of the optical spectra can indeed be explained within the strong coupling formalism. The remaining differences (for example, at high energies) can be removed by optimizing the parameters of the histogram at each particular temperature. These results are shown in the panels of figure 6 where the memory functions are calculated from $\Pi(\omega)$ functions at corresponding temperatures. The temperature dependence of $\Pi(\omega)$ is weak for the OD0 sample but becomes stronger with decreasing doping. The coupling constant, λ , can be obtained by two methods: (i) from $\lambda = m^*(\omega \to 0)/m - 1$ as discussed above and (ii) using the relation $\lambda = 2 \int_0^\infty \tilde{\Pi}(\omega) / \omega \, d\omega$. We obtained the same values with these two methods. In figure 7, we show the coupling constants derived for the Bi2201 spectra together with those derived from the other $\Pi(\omega)$ functions presented in [13]. The result shows a strong and systematic increase of λ for decreasing hole concentration. This trend can also be obtained from other probes, for example from ARPES as indicated by the crosses that are taken from [35]. The ARPES coupling constants are estimates for the nodal direction. They represent only a partial coupling constant determined from the change in dispersion around the low energy kink and are therefore smaller than the ones determined from optics. There is a trend of increasing coupling constant when the temperature is reduced. This temperature dependence becomes stronger upon decreasing the doping. The latter systematic temperature dependence of λ is a direct consequence of a growth of intensity at low energies below the 50–60 meV peak (see the $\Pi(\omega)$ functions of the UD10 sample in the left-hand panels of figure 6). As mentioned above, all trivial thermal factors contained in (2) and (3) are, in principle, folded out by our procedure. The remaining temperature dependence reflects therefore the thermal properties of the 'glue-function' itself. In a separate paper [13], we have shown for a large number of cuprates, including the present set of samples, that reasonable (albeit 2–3 times higher than experimental) values of T_c are predicted by the Eliashberg equations using these $\Pi(\omega)$ functions. Moreover, the 50–60 meV peak seems to be irrelevant for the pairing in the overdoped samples. In the Bi2201 materials T_c is low despite the fact that the electron-boson coupling found in optical and ARPES experiments is large. $\Pi(\omega)$ is, in fact, quite similar to e.g. Bi2212 and Bi2223 where the maximum T_c is of the order of 100 K. This is a natural consequence of cation disorder at the Sr site in the single layer Bi2201 compounds, suppressing rather effectively the d-wave order parameter in the copper-oxygen planes [38].

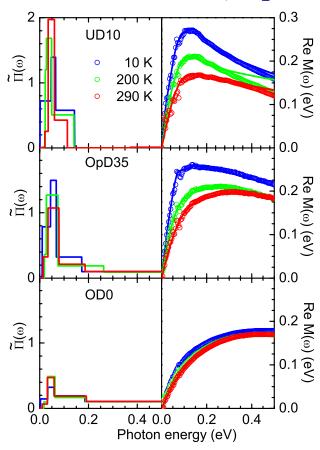


Figure 6. Left panels: $\Pi(\omega)$ functions obtained by optimizing the histogram parameters at each temperature. Right panels: corresponding $\hat{M}(\omega)$. Symbols are experiments and full lines calculations.

4. Discussion

Hwang *et al* have investigated the coupling to bosonic modes by analyzing the optical scattering rates of Bi-2212 [9, 12], [39]–[42], YBCO [43] and LSCO [44]. Several other groups have applied different methods of analysis to optical spectra with similar results but differing interpretations [45]–[54]. Several other techniques, like ARPES [35]–[37], [55]–[63] and tunneling [64]–[67], also show evidence for coupling of electrons to bosonic modes.

4.1. Comparison with other optical experiments

In most of the earlier work a spectral function consisting of two contributions is reported: a peak below 100 meV and structure in the 200–300 meV range. The doping trend of $\hat{M}(\omega)$ seen in figure 5 is similar to the one observed in [40] for Bi₂Sr₂CaCu₂O_{8+ δ}, namely that $\hat{M}(\omega)$ is a broad and featureless function for high dopings and becomes peaked and narrow for lower dopings. Hwang *et al* [12] apply an analysis similar to ours and also find an overall decrease in intensity in $\tilde{\Pi}(\omega)$ with increasing doping (note that in [12] the notation $I^2\chi(\omega)$ is used for $\tilde{\Pi}(\omega)$). The main difference is that we find the spectra to be much less temperature-dependent

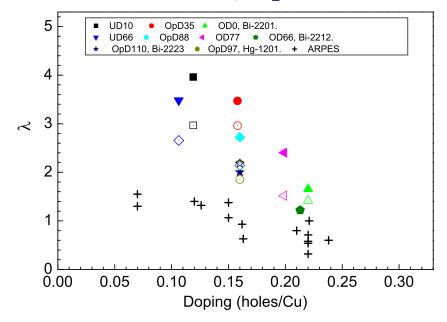


Figure 7. Coupling strength as a function of carrier concentration. Open symbols: 290 K; closed symbols: 100 K. The crosses indicate the values obtained in [35]. The observed trend of decreasing λ with doping is consistent with the one obtained by ARPES (see also [12, 36, 37]).

in the low-energy region of $\Pi(\omega)$, in agreement with the results obtained by Dordevic *et al* [52]. Hwang *et al* explain the temperature and doping dependence of these spectra as arising from the presence of a pseudogap at lower temperatures for the underdoped samples [42]. Although we cannot fully exclude this possibility, our analysis shows that another interpretation is also possible: namely the peak in $\hat{M}(\omega)$ at low doping arises from the coupling to a bosonic mode. This peak is smeared out at higher temperatures by the Bose and Fermi factors appearing in (2) and (3). The peak in $\hat{M}(\omega)$ disappears with increasing doping simply because the coupling to low-energy bosonic modes gets weaker. The temperature effect is much more pronounced for Hg1201 where the peak in $\hat{M}(\omega)$ is more clearly visible [13]. Although there is no simple relation between the energy of a peak seen in $\hat{M}(\omega)$ and the one seen in $\Pi(\omega)$, a pseudogap would shift the peak in $\hat{M}(\omega)$ to higher energies as compared with the peak in $\hat{\Pi}(\omega)$. We note that the experimental $\hat{M}(\omega)$ in figure 5 show the opposite trend, i.e. the peak in $\hat{M}(\omega)$ shifts to *lower* energy with decreasing temperature. Our analysis thus shows that features in the optical spectra that have been attributed to the opening of a pseudogap [68] can in fact be explained by a nearly temperature-independent peak in $\Pi(\omega)$ in the 50–60 meV range.

4.2. Comparison with ARPES

The experimental results from ARPES can be summarized as indicative of two distinct structures in the electron energy dispersion. Along the nodal direction one observes a kink at low energy \sim 50–70 meV [35, 37, 55, 56] followed by a 'waterfall' around 350 meV [62, 63]. The interpretation of these two features is still under debate. Along the anti-nodal direction only the low-energy feature is observed since the band bottom occurs around 100 meV. The kink has

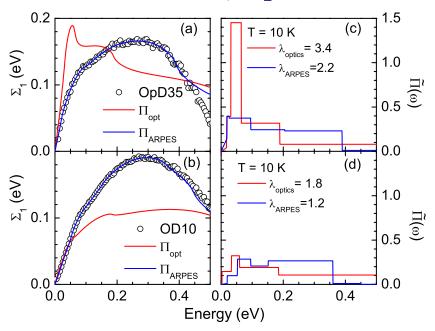


Figure 8. (a) Comparison between experimental $\Sigma(\omega)$ (open circles), calculated $\Sigma(\omega)$ from the 10 K $\Pi(\omega)$ spectra (red lines) and $\Sigma(\omega)$ obtained from a direct fit to the ARPES data (blue lines) for the OpD35 sample. (b) Same as in (a) but for the OD10 sample. (c, d) The $\Pi(\omega)$ functions corresponding to the calculated $\Sigma(\omega)$'s in the left panels. Also indicated are the total coupling constants corresponding to these spectra.

a smaller energy $\approx 40 \text{ meV}$ in the normal state and is shifted to $\approx 70 \text{ meV}$ in the superconducting state as a result of the opening of the superconducting gap [57, 58, 60, 61].

If we ignore for the moment the momentum anisotropy, then the self-energies calculated with $\Pi(\omega)$ can be compared to $\Sigma(\omega)$ extracted from ARPES. ARPES experiments have been performed on crystals taken from the same batch as used in this study [37, 69]. The self-energy along the nodal direction has been determined using a full 2D analysis of the spectral function using the LDA band structure as bare band dispersion [69]. The self-energies of the OpD35 and OD10 samples are shown in figures 8(a) and (b), respectively, by open circles. The self-energies calculated from the optical $\Pi(\omega)$ function are shown in the same figure in red. These selfenergies are quite different but a closer examination reveals that several features agree quite well. Both experiments show structure in the 50–60 meV range and display a maximum in $\Sigma(\omega)$ in the 200–300 meV range. In order to determine the experimental $\Sigma(\omega)$ from ARPES an assumption has to be made for the bare band dispersion. The fact that both the experimental and calculated self-energies have almost parallel slope in the limit of frequency going to zero suggests that at least the low-energy properties determined by optical spectroscopy and ARPES are compatible.

The ARPES self-energy can be further analyzed using our histogram model for $\Pi(\omega)$. The fit to the ARPES self-energy is shown in blue in figures 8(a) and (b). The $\Pi(\omega)$ functions obtained from optics and ARPES are compared in figures 8(c) and (d). The optical and ARPES glue-functions, although at first glance quite different, have a number of globally similar features: (i) the overall coupling strength, (ii) the broad energy range and (iii) the 50–60 meV peak. We note that the low-energy kink in the ARPES data gives rise to a peak in $\Pi(\omega)$ at the same energy as the optical data. The total coupling constants, indicated in figures 8(c) and (d), are somewhat larger for the optical $\Pi(\omega)$ function. The same trend is seen in figure 7 where we compared λ obtained from ARPES and optics for several samples. Since the optical conductivity has contributions from all of *k*-space one may expect that this explains the difference between optical and ARPES results. Stojkovic and Pines show that the optical conductivity is a linear superposition of contributions along the Fermi surface where the self-energies are *k*-dependent quantities [70],

$$\hat{\sigma}(\omega) = \frac{e^2}{8\pi^2} \int_{\text{FS}} \frac{\mathrm{d}k}{|v_{\text{f}}|} \int_{-\infty}^{+\infty} \frac{\mathrm{d}\varepsilon [f(\omega+\varepsilon,T) - f(\varepsilon,T)]}{\mathrm{i}\omega} \frac{v_{\text{f}}^2}{\omega - \Sigma_k(\varepsilon+\omega,T) + \Sigma_k^*(\varepsilon,T)}.$$
(5)

We can estimate the effect of anisotropy using our knowledge of the electronic structure from ARPES. As summarized above, the kink disperses from 70 meV at the nodal direction to 40 meV at the anti-nodal direction [71]. The second ingredient needed is the *bare* Fermi velocity, $v_{\rm f}$. Estimates of the k-dependence of v_f are available for Bi-2212 from Kaminski et al [72]. The effect of anisotropy on $\Pi(\omega)$ can now be estimated by assuming that $\hat{\sigma}(\omega)$ has two contributions: one from the nodal direction and one from the antinodal direction. We separately calculate the conductivity arising from the nodal and antinodal directions using the $\Pi(\omega)$ functions given in figures 9(a) and (b). These functions are chosen such that they are compatible with the experimental observations discussed above. The resulting conductivities are weighted with the Fermi velocity ratio $v_{f,(\pi,\pi)}$: $v_{f,(0,\pi)} = 2$: 1. The resulting optical conductivity is then analyzed using the same method as the experimental data in section 3.2. The $\Pi(\omega)$ function shown in figure 9(c) shows that the momentum anisotropy in $\Sigma(\omega)$ gives rise to a mode energy that is a weighted average of the nodal and antinodal directions. A comparison of these results with the $\Pi(\omega)$ functions from figures 8(c) and (d) shows that (i) the low energy kink seen by optics has an energy somewhat smaller than the nodal kink energy seen by ARPES and (ii) there is less intensity in the high-energy range seen by optics compared with the nodal self-energy determined from ARPES. Both effects arise because the optical $\Pi(\omega)$ function is an effective function that contains contributions from all points around the Fermi surface.

4.3. Comparison to tunneling experiments

The analysis of tunneling data for the cuprates turns out to be more complicated than for conventional superconductors. Several groups have found evidence for coupling to bosonic modes. Two groups report coupling to a mode around 40 meV [64, 65, 67]. This is significantly lower than our result. We note however that the tunneling experiments are mainly sensitive to the antinodal region of *k*-space due to the presence of a van Hove singularity. As we have seen above, ARPES experiments indicate that in the antinodal region the mode energy is indeed close to 40 meV. However, using a different analysis, Lee *et al* report coupling to a bosonic mode at 53 meV in Bi2212 [66].

5. Conclusions and outlook

The optical properties of Bi2201 show an interesting evolution with doping. The strongly underdoped UD0 sample shows a non-Drude behavior at low temperatures, while the more doped compounds all show Drude-like behavior. It is interesting to speculate at which doping

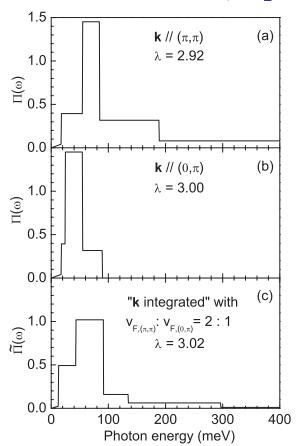


Figure 9. Estimate of the effect of *k*-space anisotropy on the optical conductivity. (a) Assumed $\Pi(\omega)$ for the nodal direction. The main peak is situated at 70 meV as reported in [35]. (b) Assumed $\Pi(\omega)$ for the antinodal direction. The main peak is situated at 40 meV as determined by ARPES [57]. Also indicated is the integrated coupling constant λ for each spectrum. (c) $\Pi(\omega)$ determined by analyzing the optical conductivity assuming contributions to $\sigma_1(\omega)$ from panels (a) and (b) weighted with a ratio of the nodal to antinodal Fermi velocity 2 : 1.

the transition from one type of low-temperature behavior to the other occurs. One possibility is that it coincides with the onset of superconductivity. An interesting consequence of our analysis is that the onset of superconductivity separates two different normal states of matter. The optical properties for higher dopings could be described within the strong coupling formalism, while the properties of the UD0 sample clearly fall in a different universality class dominated by strong electron correlations.

The strong coupling analysis shows that the coupling to bosonic modes in these materials decreases strongly as a function of doping. For the UD10 sample we find a narrow boson spectrum with a large intensity in the range below 100 meV. With increasing doping two separate trends are observed: the spectrum broadens and the coupling to the 50–60 meV peak is strongly reduced. Our study shows that the main temperature dependence of the optical spectra can be understood to arise from the thermal factors appearing in the strong coupling formalism. To consistently fit the frequency dependence at all temperatures we have to allow for temperature

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dependence in the $\tilde{\Pi}(\omega)$ function. This suggests that part of the $\tilde{\Pi}(\omega)$ spectrum is electronic in nature. Since the peak in the 50–60 meV range is present at all temperatures and has a relatively weak doping dependence, we conclude that it partially arises from vibrational degrees of freedom.

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